# Analog Systems and Applications (32221403) 

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## Unit 5:

Feedback in Amplifiers: Positive and Negative Feedback. Effect of negative feedback on Input Impedance, Output Impedance, Gain, Stability, Distortion and Noise.

## Feedback

A sampling network samples the output voltage or current and this signal is applied to the input through a feedback two port network. (Signal source can be a voltage source $\mathrm{V}_{s}$ or a current source $I_{s}$ )

- For voltage feedback, the feedback element (resistor) will be in parallel with the output.
- For current feedback the element will be in series.
- If the feedback signal is proportional to voltage, it is Voltage Feedback.
- If the feedback signal is proportional to current, it is Current Feedback.
- Conditions to be satisfied.
- Input signal is transmitted to the output through amplifier A and not through feedback network $\beta$.
- The feedback signal is transmitted to the input through feedback network and not through amplifier.
- The reverse transmission factor $\beta$ is independent of $\mathrm{R}_{s}$ and $\mathrm{R}_{L}$.

There are two types of feedback:

- Positive Feedback
- Negative Feedback (degenerative feedback)


## Advantages of Negative Feedback

- Input impedance can be increased.
- Output impedance can be decreased.
- Bandwidth is increased.
- Linearity of operation is improved.
- Distortion is reduced.
- Noise reduces.


## Effect of negative feedback on gain factor.



Figure 1: schematic for -Ve feedback.

Without negative feedback in the Fig. 1

$$
\begin{equation*}
A_{v}=\frac{V_{0}}{V_{1}} \tag{1}
\end{equation*}
$$

by including negative feedback,

$$
\begin{equation*}
A_{v}^{\prime}=V_{o} / V_{1}^{\prime} \tag{2}
\end{equation*}
$$

since

$$
\begin{gather*}
V_{1}^{\prime}=V_{1}-\beta V_{0}  \tag{3}\\
V_{0}=A_{v}\left(V_{1}-\beta V_{0}\right)  \tag{4}\\
V_{0}=A_{v}\left(V_{1}-\beta V_{0}\right)  \tag{5}\\
V_{0}=A_{v} \cdot V_{1}-A_{v} \cdot \beta V_{0}  \tag{6}\\
V_{0}\left(1+\beta A_{v}\right)=A_{v} V_{1}  \tag{7}\\
A_{v f}=\frac{V_{0}}{V_{1}}=\frac{A_{v}}{1+\beta A_{v}} \tag{8}
\end{gather*}
$$

Here $\mathrm{A}_{v f}$ is voltage gain with negative feedback.

## Reduction in Gain

For positive feedback,

$$
\begin{equation*}
A_{v}^{\prime}=\frac{A_{v}}{1-\beta A_{v}} \tag{9}
\end{equation*}
$$

$\mathrm{A}_{v}=$ voltage gain without feedback. $\beta$ is negative for negative feedback.

$$
\begin{equation*}
A_{v}^{\prime}=\frac{A_{v}}{1-\left(-\beta \cdot A_{v}\right)} \tag{10}
\end{equation*}
$$

As can be seen the denominator is greater than $1 . \mathrm{A}_{v}{ }^{\prime}$ is less than the $\mathrm{A}_{v}$. there is reduce in gain with negative feedback.

## Reduction of noise

Let N be noise constant without feedback and $\mathrm{N}_{F}$ with feedback. $\mathrm{N}_{F}$ is fed to the input and its value is $\beta \mathrm{N}_{F}$ It is amplified to $-\beta A \mathrm{~N}_{F}$. So,

$$
\begin{gather*}
N_{F}=N-\beta A N_{F}  \tag{11}\\
N_{F}=\frac{N}{1+\beta A} \tag{12}
\end{gather*}
$$

Here can be concluded that $\mathrm{N}_{F}$ is less than N , which implies tha noise is reduced with negative feedback.

- Now we will obtain expressions for gain \& impedance for the noninverting and inverting amplifier with feedback.
- when input signal is connected to the inverting ( - ) terminal of amplifier, it is inverting amplifier and when input signal is connected to the noninverting terminal $(+)$ then it is noninverting amplifier.


## Noninverting amplifier



Figure 2: Schematic for noninverting amplifier with negative feedback

Op-amp is connected in a closed loop as noninverting amplifier with controlled voltage gain. Here input signal is connected to the noninverting input. Output is connected to the
inverting terminal through feedback circuit. Feedback voltage $\left(\mathrm{V}_{f}\right)$ is $\left(\frac{R_{i}}{R_{i}+R_{f}} V_{\text {out }}\right)$. Output voltage is $\mathrm{A}_{\text {openloop }}\left(\mathrm{V}_{\text {in }}-\mathrm{V}_{f}\right)$


Figure 3: With differential input

Attenuation $(\mathrm{B})=\frac{R_{i}}{R_{i}+R_{f}}$. by putting $\mathrm{BV}_{\text {out }}$ for $\mathrm{V}_{f}$ in $\mathrm{V}_{\text {out }}$ equation.

$$
\begin{align*}
& V_{\text {out }}=A_{o l}\left(V_{\text {in }}-B V_{\text {out }}\right)  \tag{13}\\
& V_{\text {out }}=A_{o l} V_{\text {in }}-A_{o l} B V_{\text {out }}  \tag{14}\\
& V_{\text {out }}+A_{o l} B V_{\text {out }}=A_{o l} V_{\text {in }}  \tag{15}\\
& V_{\text {out }}\left(1+A_{o l} B\right)=A_{o l} V_{\text {in }} \tag{16}
\end{align*}
$$

Overall voltage gain is $\mathrm{V}_{\text {out }} / \mathrm{V}_{\text {in }}=\mathrm{A}_{o l} /\left(1+\mathrm{A}_{o l} \mathrm{~B}\right) . \mathrm{A}_{\text {ol }} \mathrm{B}$ is geater than 1.

$$
\begin{equation*}
\frac{V_{\text {out }}}{V_{\text {in }}}=\frac{A_{o l}}{A_{o l} B}=1 / B \tag{17}
\end{equation*}
$$

Closed loop gain is

$$
\begin{equation*}
A_{c l(N I)}=\frac{V_{\text {out }}}{V_{\text {in }}}=\frac{1}{B}=\frac{R_{i}+R_{f}}{R_{i}} \tag{18}
\end{equation*}
$$

So, $\mathrm{A}_{c l(N I)}=1+\frac{R_{f}}{R_{i}}$

## Voltage follower



Figure 4: Voltage follower OP-AMP

It is aspecial case where all output voltage is feedback to input. it has high iput impedance and low output impedance.

$$
\begin{equation*}
A_{c l(V F)}=1 \tag{19}
\end{equation*}
$$

## Inverting amplifier



Figure 5: Schematic for inverting amplifier with negative feedback

$$
\begin{equation*}
I_{i n}=I_{f} \tag{20}
\end{equation*}
$$



Figure 6: Virtual ground case and closed loop voltage gain for inverting amplifier.

Since there is no current at the inverting input and $\mathrm{I}_{\text {in }}=\mathrm{V}_{\text {in }} / \mathrm{R}_{i}$. Voltage across $\mathrm{R}_{f}$ is $-\mathrm{V}_{\text {out }}$. $\mathrm{I}_{f}=\frac{-V_{\text {out }}}{R_{f}}$, since $\mathrm{I}_{f}=\mathrm{I}_{i n}$,

$$
\begin{gather*}
\frac{-V_{\text {out }}}{R_{f}}=\frac{V_{\text {in }}}{R_{i}}  \tag{21}\\
A_{c l(I)}=-\frac{R_{f}}{R_{i}} \tag{22}
\end{gather*}
$$

The closed loop gain is independent of the op-amp's internal open- loop gain. negative feedback stabilizes the voltage gain.

## Impedances of a noninverting amplifier



Figure 7: Input impedance schematics

## Input Impedance

From Fig.7,

$$
\begin{equation*}
V_{i n}=V_{d}+V_{f}=V_{d}+B V_{o u t} \tag{23}
\end{equation*}
$$

Since $\mathrm{V}_{\text {out }}+\mathrm{A}_{o l} \mathrm{~V}_{d}$,

$$
\begin{equation*}
V_{i n}=V_{d}+A_{o l} B V_{d}=\left(1+A_{o l} B\right) V_{d} \tag{24}
\end{equation*}
$$

substituting $\mathrm{V}_{d}$ equal $\mathrm{I}_{i n} \mathrm{Z}_{\text {in }}$

$$
\begin{equation*}
V_{i n}=\left(1+A_{o l} B\right) I_{i n} Z_{i n} \tag{25}
\end{equation*}
$$

$Z_{i n}$ is the open loop input impedance of op-amp without feedback.

$$
\begin{gather*}
\frac{V_{i n}}{I_{i n}}=\left(1+A_{o l} B\right) Z_{i n}  \tag{26}\\
Z_{i n(N I)}=V_{i n} / I_{i n}=\left(1+A_{o l} B\right) Z_{i n} \tag{27}
\end{gather*}
$$

The above expression shows that input impedance of the noninverting amplifier with negative feedback is much greater than the input impedance of op-amp (without feedback).

## Output Impedance



Figure 8: schematics for output impedance

From Fig.8, $\mathrm{V}_{\text {out }}=\mathrm{A}_{\text {ol }} \mathrm{V}_{d}-\mathrm{Z}_{\text {out }} \mathrm{I}_{\text {out }}$. The differential input voltage $\mathrm{V}_{d}=\mathrm{V}_{\text {in }}-\mathrm{V}_{f}$, say $\mathrm{A}_{\text {ol }} \mathrm{V}_{d}$ larger than the $\mathrm{Z}_{\text {out }} \mathrm{I}_{\text {out }}$.

$$
\begin{equation*}
V_{o u t}=A_{o l}\left(V_{i n} V_{f}\right) \tag{28}
\end{equation*}
$$

by putting $\mathrm{V}_{f}$ for $\mathrm{BV}_{\text {out }}$,

$$
\begin{equation*}
V_{\text {out }}=A_{\text {ol }}\left(V_{\text {in }}-B V_{\text {out }}\right) \tag{29}
\end{equation*}
$$

by solving we get,

$$
\begin{equation*}
A_{o l} V_{\text {in }}=\left(1+A_{o l} B\right) V_{\text {out }} \tag{30}
\end{equation*}
$$

Since $\mathrm{Z}_{\text {out }(N I)}=\mathrm{V}_{\text {out }} / \mathrm{I}_{\text {out }}$. So, $\mathrm{A}_{\text {ol }} \mathrm{V}_{\text {in }}=\left(1+\mathrm{A}_{\text {ol }} \mathrm{B}\right) \mathrm{I}_{\text {out }} \mathrm{Z}_{\text {out }(N I)}$ We get,

$$
\begin{equation*}
\frac{A_{\text {ol }} V_{\text {in }}}{I_{\text {out }}}=\left(1+A_{\text {ol }} B\right) Z_{\text {out }(N I)} \tag{31}
\end{equation*}
$$

$$
\begin{array}{r}
\mathrm{A}_{\text {ol }} \mathrm{V}_{\text {in }}=\mathrm{V}_{\text {out }}, \text { So, } \mathrm{Z}_{\text {out }}=\left(1+\mathrm{A}_{\text {ol }} \mathrm{B}\right) \mathrm{Z}_{\text {out }(N I)} \text { So, } \\
\qquad Z_{\text {out }(N I)}=\frac{Z_{\text {out }}}{1+A_{o l} B} \tag{32}
\end{array}
$$

This equation shows that output impedance of the noninverting amplifier with -ve feedback is less than the internal output impedance $\mathrm{Z}_{\text {out }}$.

For Impedance for voltage follower in Fig.4, $\mathrm{Z}_{\text {in }(V F)}=\left(1+\mathrm{A}_{o l}\right) \mathrm{Z}_{\text {in }}$ and $\mathrm{Z}_{\text {out }(V F)}=$ $\mathrm{Z}_{\text {out }} /\left(1+\mathrm{A}_{\text {ol }}\right)$

## input impedance



Figure 9: schematic for input impedance

As in Fig. $9, \mathrm{Z}_{\text {in(I) }}=\mathrm{R}_{i}$, since inverting input of op-amp is at virtual ground and input
resistance is $\mathrm{R}_{i}$.

- $\mathrm{Z}_{\text {out }(I)}=\frac{Z_{\text {out }}}{1+A_{\text {ol }} B}$

Output impedance of both inverting and noninverting amplifier configuration is low, due to this near zero output impedance, any load impedance connected to the opamp output can vary greatly and not change the output votage .

Reference: Electronic Devices conventional current version by T. L. Floyd. and Electronic Devices \& circuit Theory, R.L. Boylestad \& L.D. Nashelsky, 2009, Pearson

